

Chapter 7 - Conservation of Energy + Momentum

§7-1 Energy Transformations

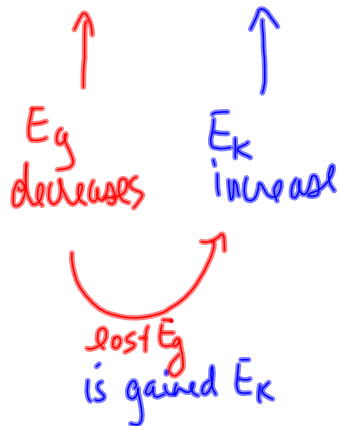
Consider a rock with 100J of gravitational potential energy:

○ $E_g = 100\text{J}$ $E_k = 0\text{J}$ $E_{\text{TOTAL}} = 100\text{J}$

○ $E_g = 65\text{J}$ $E_k = 35\text{J}$ $E_{\text{TOTAL}} = 100\text{J}$

○ $E_g = 40\text{J}$ $E_k = 60\text{J}$ $E_{\text{TOTAL}} = 100\text{J}$

○ $E_g = 0\text{J}$ $E_k = 100\text{J}$ $E_{\text{TOTAL}} = 100\text{J}$

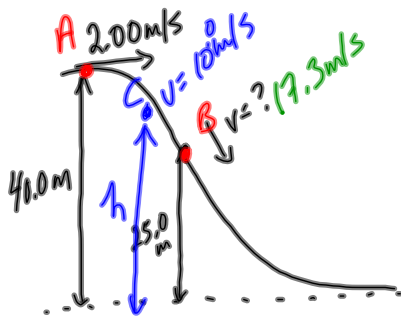


The total energy remains constant in an isolated system (i.e. neglecting friction or air resistance)

Law of Conservation of Mechanical Energy
 => The total mechanical energy in an isolated system remains constant.

$$\begin{aligned} \bar{E}_{\text{total}} &= \bar{E}'_{\text{total}} \\ \text{(before)} & \quad \text{(after)} \\ E_g + E_k + E_e &= E_g' + E_k' + E_e' \end{aligned}$$

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$$E_{total} = E'_{total}$$

(A) (B)

$$E_{gA} + E_{kA} = E_{gB} + E_{kB}$$

$$mgh_A + \frac{1}{2}mV_A^2 = mgh_B + \frac{1}{2}mV_B^2$$

$$(9.81\text{m/s}^2)(40.0\text{m}) + \frac{1}{2}(2.00\text{m/s})^2 = (9.81\text{m/s}^2)(25.0\text{m})$$

- frictionless

a) $v = ?$ when $h = 25.0\text{m}$

b) $h = ?$ when $v = 10.0\text{m/s}$

$$392.4 \frac{\text{m}^2}{\text{s}^2} + 2.00 \frac{\text{m}^2}{\text{s}^2} = 245.25 \frac{\text{m}^2}{\text{s}^2} + \frac{1}{2}V_B^2$$

$$149.15 \frac{\text{m}^2}{\text{s}^2} = \frac{1}{2}V_B^2$$

$$V_B^2 = 2(149.15 \frac{\text{m}^2}{\text{s}^2})$$

$$V_B = 17.3 \text{m/s}$$

b) $E_{total} = E'_{total}$

(A) (C)

$$E_{gA} + E_{kA} = E_{gC} + E_{kC}$$

$$mgh_A + \frac{1}{2}mV_A^2 = mgh_C + \frac{1}{2}mV_C^2$$

$$gh_A + \frac{1}{2}V_A^2 = gh_C + \frac{1}{2}V_C^2$$

$$(9.81\text{m/s}^2)(40.0\text{m}) + \frac{1}{2}(2.00\text{m/s})^2 = (9.81\text{m/s}^2)(h_C) + \frac{1}{2}(10.0\text{m/s})^2$$

$$392.4 \frac{\text{m}^2}{\text{s}^2} + 2.00 \frac{\text{m}^2}{\text{s}^2} = (9.81\text{m/s}^2)h_C + 50.0 \frac{\text{m}^2}{\text{s}^2}$$

$$344.4 \frac{\text{m}^2}{\text{s}^2} = (9.81\text{m/s}^2)h_C$$

$$h_C = 35.1\text{m}$$

To DO: PP/287